

TABLE 8.14-5 Formulas for Testing Simple Effects

(i) AB interaction significant: Error Term ($A, B,$ and C Fixed Effects, Subjects Random)

$$SS_A \text{ at } b_1 = \sum_1^p \frac{(AB_{i1})^2}{nr} - \frac{\left(\sum_1^p B_{i1}\right)^2}{npr} \quad \frac{MS_{\text{subj w. groups}} + MS_{B \times \text{subj w. groups}}(q-1)}{q}$$

$$SS_B \text{ at } a_1 = \sum_1^q \frac{(AB_{1j})^2}{nr} - \frac{\left(\sum_1^q A_{1j}\right)^2}{nqr} \quad MS_{B \times \text{subj w. groups}}$$

(ii) AC interaction significant:

$$SS_A \text{ at } c_1 = \sum_1^p \frac{(AC_{i1})^2}{nq} - \frac{\left(\sum_1^p C_{i1}\right)^2}{npq} \quad \frac{MS_{\text{subj w. groups}} + MS_{C \times \text{subj w. groups}}(r-1)}{r}$$

$$SS_C \text{ at } a_1 = \sum_1^r \frac{(AC_{1k})^2}{nq} - \frac{\left(\sum_1^r A_{1k}\right)^2}{nqr} \quad MS_{C \times \text{subj w. groups}}$$

(iii) BC interaction significant:

$$SS_B \text{ at } c_1 = \sum_1^q \frac{(BC_{j1})^2}{np} - \frac{\left(\sum_1^q C_{j1}\right)^2}{npq} \quad \frac{MS_{B \times \text{subj w. groups}} + MS_{BC \times \text{subj w. groups}}(r-1)}{r}$$

$$SS_C \text{ at } b_1 = \sum_1^r \frac{(BC_{1k})^2}{np} - \frac{\left(\sum_1^r B_{1k}\right)^2}{npr} \quad \frac{MS_{C \times \text{subj w. groups}} + MS_{BC \times \text{subj w. groups}}(q-1)}{q}$$

(iv) ABC interaction significant:

$$SS_A \text{ at } bc_{11} = \sum_1^p \frac{(ABC_{i11})^2}{n} - \frac{(BC_{11})^2}{np} \quad MS_{\text{w. cell}}$$

$$SS_B \text{ at } ac_{11} = \sum_1^q \frac{(ABC_{1j1})^2}{n} - \frac{(AC_{11})^2}{nq} \quad \frac{MS_{B \times \text{subj w. groups}} + MS_{BC \times \text{subj w. groups}}(r-1)}{r}$$

$$SS_C \text{ at } ab_{11} = \sum_1^r \frac{(ABC_{11k})^2}{n} - \frac{(AB_{11})^2}{nr} \quad \frac{MS_{C \times \text{subj w. groups}} + MS_{BC \times \text{subj w. groups}}(q-1)}{q}$$

$$SS_{AB} \text{ at } c_1 = \left[\sum_1^p \sum_1^q \frac{(ABC_{ij1})^2}{n} - \frac{\left(\sum_1^p C_{i1}\right)^2}{npq} \right] - SS_A \text{ at } c_1 - SS_B \text{ at } c_1 \quad \frac{MS_{B \times \text{subj w. groups}} + MS_{BC \times \text{subj w. groups}}(r-1)}{r}$$

$$SS_{AC} \text{ at } b_1 = \left[\sum_1^p \sum_1^r \frac{(ABC_{i1k})^2}{n} - \frac{\left(\sum_1^p B_{i1}\right)^2}{npr} \right] - SS_A \text{ at } b_1 - SS_C \text{ at } b_1 \quad \frac{MS_{C \times \text{subj w. groups}} + MS_{BC \times \text{subj w. groups}}(q-1)}{q}$$

$$SS_{BC} \text{ at } a_1 = \left[\sum_1^q \sum_1^r \frac{(ABC_{1jk})^2}{n} - \frac{\left(\sum_1^q A_{1j}\right)^2}{nqr} \right] - SS_B \text{ at } a_1 - SS_C \text{ at } a_1 \quad MS_{BC \times \text{subj w. groups}}$$