

Table 19.5

Illustrative data for a two-factor experiment with repeated measurements on one factor

		Subjects	C ₁	C ₂	C ₃	C ₄	C ₅	T _{r,s}
Group 1	R ₁	1	2	7	6	7	9	31
		2	4	3	7	12	14	40
		3	7	6	4	12	10	39
		4	1	3	3	6	6	19
		T _{re.}	14	19	20	37	39	T _{1..} = 129
Group 2	R ₂	1	4	4	7	9	1	25
		2	10	12	12	12	16	62
		3	8	7	8	12	10	45
		4	5	7	6	7	8	33
		T _{re.}	27	30	33	40	35	T _{2..} = 165
	T _{c.}	41	49	53	77	74	T = 294	

From this table six quantities can be readily calculated as follows:

$$\frac{1}{C} \sum^R \sum^n T_{r,s}^2 = \frac{1}{4} [(31)^2 + (40)^2 + \dots + (33)^2] = 2,405.20$$

$$\frac{1}{nC} \sum^R T_{r..}^2 = \frac{1}{4 \times 5} [(129)^2 + (165)^2] = 2,193.30$$

$$\frac{1}{nR} \sum^C T_{.c.}^2 = \frac{1}{4 \times 2} [(41)^2 + (49)^2 + \dots + (74)^2] = 2,287.00$$

$$\frac{1}{n} \sum^R \sum^C T_{re.}^2 = \frac{1}{4} [(14)^2 + (19)^2 + \dots + (35)^2] = 2,347.50$$

$$\sum^R \sum^C \sum^n X_{rei}^2 = (2)^2 + (7)^2 + \dots + (8)^2 = 2,664.00$$

$$\frac{T^2}{nRC} = \frac{(294)^2}{4 \times 2 \times 5} = 2,160.90$$

Applying the computation formulas given in Sec. 19.8, the required sums of squares are as follows:

BETWEEN SUBJECTS

$$\frac{1}{C} \sum^R \sum^n T_{r,s}^2 - \frac{T^2}{nRC} = 2,405.20 - 2,160.90 = 244.30$$

ROWS

$$\frac{1}{nC} \sum^R T_{r..}^2 - \frac{T^2}{nRC} = 2,193.30 - 2,160.90 = 32.40$$